**PHY1506**

( 478699)

May/June 2018

**Electromagnetism and Heat (Fisika)**

Duration 2 Hours

100 Marks

**EXAMINERS**

FIRST

SECOND

DR B MUKERU

PROF BM MOTHUDI

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**Use of a non-programmable pocket calculator is permissible****Closed book examination****This examination question paper remains the property of the University of South Africa and may not be removed from the examination venue****INSTRUCTIONS:**

- This paper consists of 9 pages.
- The paper consists of 2 sections (A and B) for a maximum of 100 marks.
- Marks for each question or part are indicated in brackets on the right of the question
- Show all the necessary steps in carrying out your calculations
- Page 9 contains useful formulas
- For both sections, answer **ALL** questions in the answer book.

[TURN OVER]

**Section A (Multiple choice questions)**

(Each question carries 3 marks TOTAL [30])

1) The ideal-gas law  $pV = nRT$  can be transformed into  $pV = Nk_B T$  if

(1)  $n = \frac{R}{N}$  and  $k_B = \frac{R}{N_A}$

(2)  $R = \frac{n}{N_A}$  and  $k_B = \frac{N_A}{R}$

(3)  $n = \frac{N}{N_A}$  and  $k_B = \frac{R}{N_A}$

(4)  $n = \frac{N_A}{N}$  and  $R = \frac{n}{N_A}$

(5) None of the above

2) The equation of the mean free path  $\lambda$  is given by  $\lambda = \frac{1}{4\sqrt{2}\pi(N/V)r^2}$ . Solving this equation for  $r$  one obtains

(1)  $r = \frac{1}{2\sqrt{\sqrt{2}\pi(N/V)\lambda}}$

(2)  $r = \frac{1}{4\sqrt{\sqrt{2}\pi(N/V)\lambda}}$

(3)  $r = \frac{\lambda}{4\sqrt{\sqrt{2}\pi(N/V)}}$

(4)  $r = \frac{\frac{N}{V}}{4\sqrt{\sqrt{2}\pi}}$

(5) None of the above

3) The following mathematical equation  $\vec{B} = \frac{\mu_0}{4\pi\epsilon_0} \frac{q\vec{v} \times \hat{r}}{r^2}$  represents one of the following laws

(1) Biot-Savart law

(2) Lenz's law

(3) Second law of thermodynamics

(4) Faraday's law

(5) None of the above

[TURN OVER]

- 4) When a fixed amount of ideal gas goes through an isothermal expansion
- (1) its internal (thermal) energy does not change,
  - (2) the gas does no work,
  - (3) no heat enters or leaves the gas
  - (4) its temperature must decrease,
  - (5) none of the above
- 5) A point charge  $q$  is located a short distance from a point charge  $3q$ , and no other charges are present. If the electrical force on  $q$  is  $F$  what is the electrical force on  $3q$  when the distance between the two charges is reduced half ?
- (1)  $4F$
  - (2)  $\frac{F}{4}$ ,
  - (3)  $F$ ,
  - (4)  $\frac{\sqrt{4}}{F}$ ,
  - (5) none of the above
- 6) If a current of 2.4 A is flowing in a cylindrical wire of diameter 2.0 mm, what is the average current density in this wire?
- (1)  $5.2 \times 10^{-6} \text{ A/m}^2$ ,
  - (2)  $7.6 \times 10^5 \text{ A/m}^2$ ,
  - (3)  $1.9 \times 10^5 \text{ A/m}^2$ ,
  - (4)  $3.6 \times 10^5 \text{ A/m}^2$ ,
  - (5) none of the above

[TURN OVER]

7) Some of the following statements represent Kirchhoff's loop laws

- (1) An equipotential surface due to an electrode must roughly match the shape of the electrode
- (2) The sum of currents entering a junction is equal to the sum of currents leaving the junction
- (3) There is an induced current in a closed, conducting loop if and only if the current is such that the induced magnetic field opposes the change in the flux
- (4) The sum of all the potential differences in a closed path is zero
- (5) (2) and (4) are correct

8) The potential of a ring of radius  $R$  and charge  $Q$  is given by  $V_{\text{ring}} = \frac{1}{4\pi\epsilon_0} \frac{Q}{\sqrt{z^2 + R^2}}$ . The  $z$ -component of the corresponding electric field  $E_z$  is

(1)  $E_z = \frac{1}{4\pi\epsilon_0} \frac{Q}{(z^2 + R^2)^{3/2}}$

(2)  $E_z = \frac{1}{4\pi\epsilon_0} \frac{zQ}{(z^2 + R^2)^{3/2}}$

(3)  $E_z = \frac{1}{4\pi\epsilon_0} \frac{z^2Q}{(z^2 + R^2)^{5/2}}$

(4)  $E_z = 0$

(5) None of the above

9) In an  $LR$  circuit, the current is given by  $I = I_0 e^{-t/\tau}$ , where  $\tau$  is the time constant. Solving this equation for  $t$ , we obtain

(1)  $t = -\tau \ln\left(\frac{I}{I_0}\right)$

(2)  $t = \tau \ln\left(\frac{I}{I_0}\right)$

(3)  $t = -\frac{1}{\tau} \ln\left(\frac{I}{I_0}\right)$

(4)  $t = -\tau \frac{I}{I_0}$

(5) None of the above

[TURN OVER]

10) Which one of the following statements is incorrect?

- (1) In an *LRC* circuit, the resonance occurs when  $\omega L = \frac{1}{\omega C}$
- (2) The resonance frequency is given by  $\omega_0 = \frac{1}{\sqrt{LC}}$
- (3) At resonance, the current an *RLC* circuit is minimum
- (4) The phase angle is  $0^\circ$  at resonance
- (5) All the statements above are incorrect

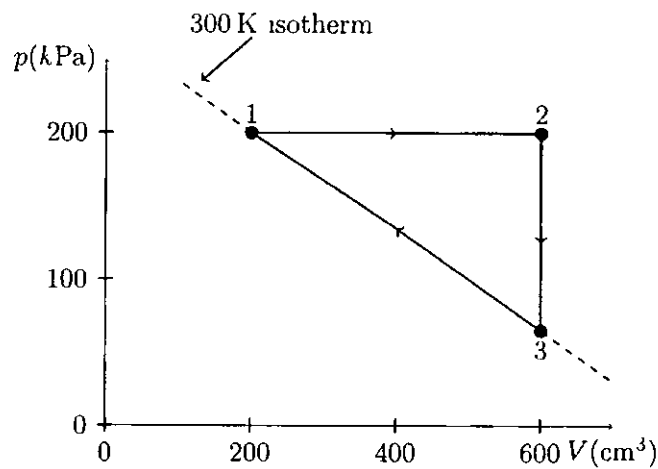
[TURN OVER]

SECTION B (Written solutions)

Question 1

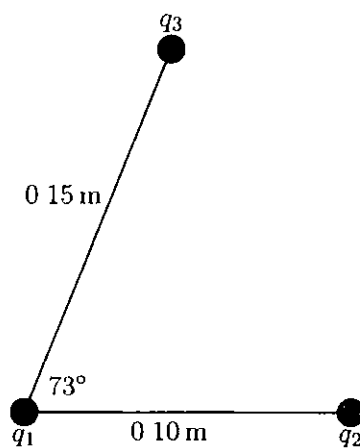
Analyze the heat engine of the figure below to determine

- (a) the net work done per cycle ( $W_{\text{out}}$ ) (12)  
(b) the engine's thermal efficiency The engine contains a monoatomic ideal gas (8)  
[20]



Question 2

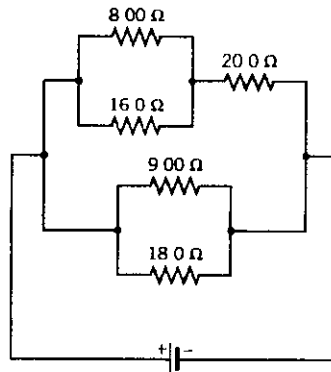
The figure below shows three point charges that lie in the  $x,y$  plane. Determine the magnitude and direction of the net electrostatic force on  $q_1$ , if  $q_1 = +4 \mu\text{C}$ ,  $q_2 = -6 \mu\text{C}$  and  $q_3 = -5 \mu\text{C}$  [10]



[TURN OVER]

### Question 3

The drawing below shows an electric circuit, where resistors are connected to a battery. If the current in the  $8.0\ \Omega$  resistor is  $0.5\ \text{A}$ , calculate



- (a) the equivalent resistance, (6)
- (b) the current in each resistor, (6)
- (c) the total current flowing in the circuit, (3)
- (d) the voltage of the battery, (3)
- (e) the electric power of the circuit (2)

[20]

Please summarize your results in a table for a better reading

### Question 4

An AM radio antenna picks up a  $1000\ \text{kHz}$  signal with a peak voltage of  $5.0\ \text{mV}$ . The tuning circuit consists of a  $60\ \mu\text{H}$  inductor in series with a variable capacitor. The inductor coil has a resistance of  $0.25\ \Omega$ , and the resistance of the rest of the circuit is negligible.

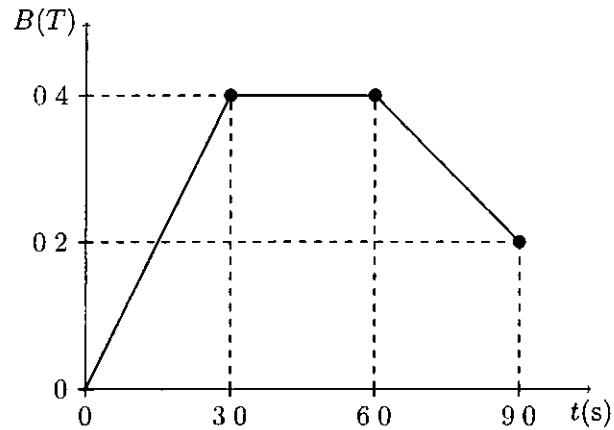
- (a) To what value should the capacitor be tuned to listen to this radio station? (Note that the capacitor needs to be tuned to where it is in resonance with the inductor) (4)
- (b) Calculate the peak current through the circuit at resonance (3)
- (c) A stronger station at  $1050\ \text{kHz}$  produces  $10\ \text{mV}$  antenna signal. Calculate the current at this frequency and the corresponding phase angle when the radio is tuned to  $1000\ \text{kHz}$  (4)

[10]

[TURN OVER]

### Question 5

A magnetic field passes through a stationary wire loop, and its magnitude changes in time according to the graph in the drawing. The direction of the field remains constant however. There are three equal time intervals indicated in the graph: 0 – 3.0 s, 3.0 – 6.0 s, and 6.0 – 9.0 s. The loop consists of 50 turns of wire and has an area of  $0.15 \text{ m}^2$ . The magnetic field is oriented parallel to the normal to the loop (i.e. the angle  $\phi = 0^\circ$ ).



- (a) For each interval, determine the induced emf (5)
- (b) The wire has a resistance of  $0.50 \Omega$ . Determine the induced current for the first and last intervals (5)
- [10]

**TOTAL: 70 MARKS**  
**[TURN OVER]**



## FORMULAE

$$PV = nRT$$

$$U_{\text{el}} = \frac{kq}{r}, \quad F = \frac{kq_1q_2}{r^2}$$

$$E_r = -\frac{dV}{dr}$$

$$Q_C + W_{\text{out}} = Q_H$$

$$R = R_1 + R_2$$

$$f = \frac{\omega}{2\pi}$$

$$V_R = IR$$

$$X_C = \frac{1}{\omega C}$$

$$Q_P = nC_P \Delta T$$

$$W = p\Delta V$$

$$\Delta E_{\text{th}} = Q - W$$

$$\frac{P_i V_i}{T_i} = \frac{P_f V_f}{T_f}$$

$$Q = mC\Delta T$$

$$Q_H = \frac{W_{\text{out}}}{\eta}$$

$$J = \frac{I}{A}$$

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$\omega_0 = \frac{1}{\sqrt{LC}}$$

$$I = \frac{\mathcal{E}_0}{\sqrt{R^2 + (X_L + X_C)^2}}$$

$$V_C = IX_C, \quad \mathcal{E} = -N \frac{\Delta\Phi}{\Delta t}, \quad \Phi = AB \cos \phi$$

$$Q_V = nC_V \Delta T$$

$$W = nRT \ln(V_f/V_i) \text{ (isothermal)}$$

$$\Delta E_{\text{th}} = Q$$

$$\Delta E_{\text{th}} = \eta C_V \Delta T \text{ (any process)}$$

$$E_{\text{th}} = \frac{5}{2} nRT \text{ (diatomic gas)}$$

## USEFUL INFORMATION

$$k_B = 1.38 \times 10^{-23} \text{ J/K}$$

$$e = 1.60 \times 10^{-19} \text{ C}$$

$$K = 9.0 \times 10^9 \text{ Nm}^2/\text{C}^2$$

$$C_P = \frac{5}{2}R, \quad C_V = \frac{3}{2}R \text{ (monoatomic ideal gas)}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ Tm/A}$$

$$N_A = 6.02 \times 10^{23} \text{ mol}^{-1}$$

$$R = 8.31 \text{ J/mol K}$$

$$1 \mu\text{C} = 10^{-6} \text{ C}$$

**PART 1 (GENERAL/ALGEMEEN)-DEEL 1**

STUDY UNIT (BY PSY100-X) / STUDIE EENHEID (BY PSY100-X)

INITIALS AND SURNAME (VOORLETTERS EN VAN)

DATE OF EXAMINATION (DATUM VAN EKSAMEN)

PAPER NUMBER (VRAESTELNOMMER)

STUDENT NUMBER (STUDENTNOMMER)

UNIQUE PAPER NO (UNIEKE VRAESTEL NR)

EXAMINATION CENTRE (E.G. PRETORIA) / EKSAMENSENTRUM (BY PRETORIA)

1 2 3 4 5 6 7 8 9

For use by examination invigilator  
 Vir gebruik deur eksamenopsiener

**IMPORTANT** **BELANGRIK**

- USE ONLY AN HB PENCIL TO COMPLETE THIS SHEET
- MARK LIKE THIS
- CHECK THAT YOUR INITIALS AND SURNAME HAS BEEN FILLED IN CORRECTLY
- ENTER YOUR STUDENT NUMBER FROM LEFT TO RIGHT
- CHECK THAT YOUR STUDENT NUMBER HAS BEEN FILLED IN CORRECTLY
- CHECK THAT THE UNIQUE NUMBER HAS BEEN FILLED IN CORRECTLY
- CHECK THAT ONLY ONE ANSWER PER QUESTION HAS BEEN MARKED
- DO NOT FOLD
- GEbruik slegs 'n HB potlood om hierdie blad te voltooi
- Merk as volg
- Kontroleer dat u voorletters en van reg ingevul is
- Vul u studentnommer van links na regs in
- Kontroleer dat u die korrekte studentnommer verstrek het
- Kontroleer dat die unieke nommer reg ingevul is
- Maak seker dat net een alternatief per vraag gemerk is
- Moenie vou nie

**PART 2 (ANSWERS/ANTWOORDE)-DEEL 2**

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140
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**Specimen only**

## MARK READING SHEET INSTRUCTIONS

Your mark reading sheet is marked by computer and should therefore be filled in thoroughly and correctly

### USE ONLY AN HB PENCIL TO COMPLETE YOUR MARK READING SHEET

*PLEASE DO NOT FOLD OR DAMAGE YOUR MARK READING SHEET*

Consult the illustration of a mark reading sheet on the reverse of this page and follow the instructions step by step when working on your sheet

Instruction numbers ① to ⑩ refer to spaces on your mark reading sheet which you should fill in as follows

- ① Write your paper code in these eight squares, for instance

P	S	Y	1	0	0	-	X
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- ② The paper number pertains only to first-level courses consisting of two papers

WRITE 

0	1
---	---

 for the first paper and 

0	2
---	---

 for the second. If only one paper, then leave blank

- ③ Fill in your initials and surname
- ④ Fill in the date of the examination
- ⑤ Fill in the name of the examination centre
- ⑥ WRITE the digits of your student number HORIZONTALLY (from left to right). Begin by filling in the first digit of your student number in the first square on the left, then fill in the other digits, each one in a separate square
- ⑦ In each vertical column mark the digit that corresponds to the digit in your student number as follows [-]
- ⑧ WRITE your unique paper number HORIZONTALLY  
NB Your unique paper number appears at the top of your examination paper and consists only of digits (e.g. 403326)
- ⑨ In each vertical column mark the digit that corresponds to the digit number in your unique paper number as follows [-]
- ⑩ Question numbers 1 to 140 indicate corresponding question numbers in your examination paper. The five spaces with digits 1 to 5 next to each question number indicate an alternative answer to each question. The spaces of which the number correspond to the answer you have chosen for each question and should be marked as follows [-]
- ◆ For official use by the invigilator. Do not fill in any information here